



# Continuous-Time Optimal Portfolio Selection Using Mean-CaR Models

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Received: July 18, 2005; Revised: October 22, 2006

**Abstract:** This paper studies continuous-time optimal portfolio selection under the setting of Black-Scholes financial markets and constant re-balanced portfolio (CRP) investment strategies. Three mean-CaR models are formulated, which minimize the risk measured by capital-at-risk (CaR) under the constraint that the expected terminal wealth is not lower than a pre-assigned level. These models are converted into bi-level optimization problems by virtue of a decomposition of the feasible solution set and, as a result, explicit optimal strategies and efficient frontiers are obtained in closed-form. A comparison of the three mean-CaR models and a numerical example illustrating the results are presented. Some economic implications of the results are also examined.

**Keywords:** *Continuous-time portfolio selection; Capital-at-Risk (CaR); Black-Scholes financial markets; constant-rebalanced portfolios (CRP); mean-CaR models.*

**Mathematics Subject Classification (2000):** 91B28, 91B62, 90B50, 90C90, 49M37.